

**PROCEEDINGS
of the
Research Experiences for Undergraduates
Program in Mathematics**

**Oregon State University
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Dennis J. Garity, Director

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William Black..... Oregon State University	David Koop..... Calvin College
Michael Censer..... New College, Florida	Rachel Lash..... Alfred University
Christine Devena Oregon State University	Sarah Lobser Smith College
Courtney Fitzgerald Niagara University	Timothy Ritter..... Bethel College
Christian Grostic..... Kalamazoo College	Ellen Veomett Univ. of Nebraska at Lincoln

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